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Geometry of the shears mechanism in nuclei

P. Van Isacker¹ and A.O. Macchiavelli²

¹Grand Accélérateur National d'Ions Lourds, CEA/DSM-CNRS/IN2P3,

B.P. 55027, F-14076 Caen Cedex 5, France and

²Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720

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The geometry of the shears mechanism in nuclei is derived from the nuclear shell model. This is achieved by taking the limit of large angular momenta (classical limit) of shell-model matrix elements.

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A central theme in the study of quantum many-body systems is the understanding of its elementary modes of excitation. Of particular interest is the competition between single-particle and collective degrees of freedom. In general, single-particle motion gives rise to irregular level sequences, associated with the unique properties of the individual particles. Collective motion generates more regular structures, a typical example being that of rotational bands which follow closely a J(J + 1) sequence, characteristic of a quantum rotor.

In atomic nuclei, the energy scales of these modes are somewhat comparable, leading to a rich and complex structure [1]. ²⁰⁸Pb is considered a paradigm of a doublyclosed-shell nucleus with collective states based on an octupole phonon. Neighboring nuclei provided a wealth of important information for the shell model, on singleparticle levels and residual interactions at the Z = 82, N = 126 shell closure, as well as on the role of particlevibration coupling [2].

The observation in ¹⁹⁹Pb of a regular sequence of γ rays resembling, at first look, a rotational band came as a surprise [3–6]. A closer inspection of the data established that these transitions were of magnetic character, in contrast to the quadrupole nature in the well-known nuclear rotors [1]. The answer to this puzzle was provided by Frauendorf [7], who based on the Titled Axis Cranking Model proposed the so-called "shears mechanism". He showed that for a weakly deformed system, there exist low-energy configurations in which neutrons and protons combine into stretched structures ("blades") and the angular momentum is generated by the re-coupling of these blades, resembling the closing of a pair of shears. As discussed in Ref. [8], the breaking of the rotational symmetry in this case originates in an anisotropic distribution of nucleonic current loops (rather than electric charge), and thus it is usually referred as magnetic rotation. Further experiments not only confirmed this picture in the lead region, but also established the mechanism in other regions of the Segré chart, near doubly-magic closures.

While an interpretation in terms of the shears mechanism provides an appealing, intuitive picture of these nuclear states, the question remains whether this geometric character is borne out by microscopic calculations. In numerical shell-model calculations Frauendorf *et al.* [9] showed that the shears picture is valid in the lead isotopes. A direct derivation of the geometry of the shears mechanism from the shell model has, however, to our knowledge never been given. Providing such a derivation is the purpose of the present Letter.

Let us assume that two nucleons of one type (say neutrons) occupy particle-like orbits $j_{1\nu}$ and $j_{2\nu}$, while two nucleons of the other type (protons) occupy hole-like orbits $j_{1\pi}^{-1}$ and $j_{1\pi}^{-1}$ [10]. The neutrons and protons are coupled to angular momenta J_{ν} and J_{π} , respectively, which are close to stretched, $J_{\rho} \approx j_{1\rho} + j_{2\rho}$ ($\rho = \nu, \pi$). The two-particle (2p) and two-hole (2h) states are represented as $|N\rangle = |j_{1\nu}j_{2\nu}; J_{\nu}\rangle$ and $|P^{-1}\rangle = |j_{1\pi}^{-1}j_{2\pi}^{-1}; J_{\pi}\rangle$, and we assume that the states are Pauli allowed, *i.e.*, that J_{ρ} is even if $j_{1\rho} = j_{2\rho}$. A shears band consists of the states $|NP^{-1}; J\rangle$ where J results from the coupling of J_{ν} and J_{π} .

We ask the following questions: How do the energies of the members of this band evolve as a function of J, and how does this evolution depends on the angular momenta of the single-particle orbits and the angular momenta of the blades? We answer these questions by adopting a shell-model hamiltonian of the generic form $H = H_{\nu} +$ $H_{\pi} + V_{\nu\pi}$ and computing $\langle NP^{-1}; J|H|NP^{-1}; J \rangle$, which will be referred to as the (2p-2h) shears matrix element.

The shell-model hamiltonian is specified by the singleparticle energies, the single-hole energies, the neutronneutron and proton-proton (two-body) interaction matrix elements, and the neutron-proton (np) interaction matrix elements $V_{j\nu j\pi}^R \equiv \langle j_\nu j_\pi; R | V_{\nu\pi} | j_\nu j_\pi; R \rangle$. One finds that the energy contribution of H_{ν} and H_{π} is constant for all members of the shears band and that any J dependence originates from the np interaction $V_{\nu\pi}$. A multipole expansion of the latter interaction leads to the following expression for the shears matrix element:

$$\langle NP^{-1}; J | V_{\nu\pi} | NP^{-1}; J \rangle$$

$$= -\mathcal{P} \hat{J}_{\nu} \hat{J}_{\pi} \sum_{R} \hat{R} V^{R}_{j_{1\nu}j_{1\pi}} \begin{cases} j_{1\nu} & J_{\nu} & J_{\pi} & j_{1\pi} \\ j_{2\nu} & J & j_{2\pi} & R \\ j_{1\nu} & J_{\nu} & J_{\pi} & j_{1\pi} \end{cases} , (1)$$

where $\hat{x} \equiv 2x + 1$ and $\mathcal{P} \equiv \mathcal{P}_{\nu}\mathcal{P}_{\pi}$ with \mathcal{P}_{ρ} an operator defined from $\mathcal{P}_{\rho}f(j_{1\rho}, j_{2\rho}) = f(j_{1\rho}, j_{2\rho}) + f(j_{2\rho}, j_{1\rho})$ for any function f. The object in curly brackets is a 12jsymbol of the *first* kind, a quantity which is scalar under rotations and depends on twelve angular momenta. The result (1) is obtained by expressing the shears matrix element as a sum over four 6j symbols, which can be related to a 12j symbol, see Eq. (19.1) of Ref. [11].

It is now a simple matter to introduce in the sum (1) values for the np interaction matrix elements and to derive the J dependence of the shears matrix element. For any reasonable nuclear interaction and for $J_{\rho} \approx j_{1\rho} + j_{2\rho}$, it is found that the sum (1) has an approximate parabolic behavior around its minimum around $J^2 \approx J_{\nu}^2 + J_{\pi}^2$.

To understand better this numerical finding, the geometry of the expression (1) can be studied by taking the limit of large angular momenta in the recoupling coefficients. Such limits are known since the seminal study of Wigner on the classical limit of 3j and 6j symbols (see chapter 27 of Ref. [12]), subsequently refined by Ponzano and Regge [13] whose work was put on a mathematically solid footing by Schulten and Gordon [14]. The classical limit of a 3j symbol is associated with the area of a (projected) triangle while that of a 6j symbol involves the volume of a tetrahedron, with the lengths of the sides determined by the angular momenta. Classical limits not only yield approximate expressions for (re)coupling coefficients but in addition provide an insight into their geometrical significance. The study of the classical limit of 3nj symbols with n > 2 is still a topic of active research with ramifications in fields as diverse as quantum gravity and quantum computing (see, *e.g.* Refs. [15–17] and references therein), well beyond the standard applications in, for example, atomic or nuclear physics.

Since at this moment only partial results are known for 9j (let alone 12j) symbols, a classical limit of the expression (1) for arbitrary interactions is difficult to obtain. We consider instead the surface delta interaction (SDI) [18], $V^{\text{SDI}}(i,j) = -4\pi a'_T \delta(\bar{r}_i - \bar{r}_j) \delta(r_i - R)$, which is known to be a reasonable approximation to the nucleonnucleon interaction [19]. The np matrix element $V^R_{j_{\nu}j_{\pi}}$ of the SDI is [18]

$$-\frac{\hat{j}_{\nu}\hat{j}_{\pi}}{2} \left[a_{01} \left(\begin{array}{cc} j_{\nu} & j_{\pi} & R \\ \frac{1}{2} & -\frac{1}{2} & 0 \end{array} \right)^2 + a_0 \left(\begin{array}{cc} j_{\nu} & j_{\pi} & R \\ \frac{1}{2} & \frac{1}{2} & -1 \end{array} \right)^2 \right], \quad (2)$$

with $a_{01} = (a_0 + a_1)/2 - (-)^{\ell_{\nu} + \ell_{\pi} + R} (a_0 - a_1)/2$ in terms of the strengths $a_T = a'_T C(R_0)$, where $C(R_0)$ equals $R^4_{n_{\nu}\ell_{\nu}}(R_0)R^2_0 = R^4_{n_{\pi}\ell_{\pi}}(R_0)R^2_0.$

When the SDI np matrix elements (2) are introduced in the shears matrix element (1), one encounters sums of the type

$$\sigma_n^{(\lambda)} \equiv (2J_\nu + 1)(2J_\pi + 1) \sum_R (-)^{\lambda R} (2R + 1) \left(\begin{array}{cc} j_{1\nu} & j_{1\pi} & R\\ \frac{1}{2} & n - \frac{1}{2} & -n \end{array} \right)^2 \begin{cases} j_{1\nu} & J_\nu & J_\pi & j_{1\pi}\\ j_{2\nu} & J & j_{2\pi} & R\\ j_{1\nu} & J_\nu & J_\pi & j_{1\pi} \end{cases} ,$$
(3)

for $(\lambda, n) = (0, 0)$, (0, 1) and (1, 0). These reduce to simple expressions in the classical limit. For example, for $\lambda = 0$, the sum can be exactly rewritten as

$$\sigma_n^{(0)} = (2J_\nu + 1)(2J_\pi + 1) \sum_{\substack{m_\nu M_\nu \\ m_\pi M_\pi}} \left(\begin{array}{cc} j_{1\nu} & j_{2\nu} & J_\nu \\ \frac{1}{2} & m_\nu & M_\nu \end{array} \right)^2 \left(\begin{array}{cc} j_{1\pi} & j_{2\pi} & J_\pi \\ -n + \frac{1}{2} & m_\pi & M_\pi \end{array} \right)^2 \left(\begin{array}{cc} J_\nu & J_\pi & J \\ M_\nu & M_\pi & m_\nu + m_\pi - n + 1 \end{array} \right)^2.$$
(4)

The classical approximation consists of replacing the last 3j symbol in Eq. (4) according to [12]

$$\left(\begin{array}{cc}J_{\nu} & J_{\pi} & J\\M_{\nu} & M_{\pi} & M\end{array}\right)^2 \mapsto \left(4\pi A_{M_{\nu}M_{\pi}M}^{J_{\nu}J_{\pi}J}\right)^{-1},\qquad(5)$$

where $A_{M_{\nu}M_{\pi}M}^{J_{\nu}J_{\pi}J}$ is related to the Caley determinant,

$$\left(A_{M_{\nu}M_{\pi}M}^{J_{\nu}J_{\pi}J} \right)^2 = -\frac{1}{16} \begin{vmatrix} 0 & a_{J_{\nu}M_{\nu}} & a_{J_{\pi}M_{\pi}} & 1 \\ a_{J_{\nu}M_{\nu}} & 0 & a_{JM} & 1 \\ a_{J_{\pi}M_{\pi}} & a_{JM} & 0 & 1 \\ 1 & 1 & 1 & 0 \end{vmatrix},$$
 (6)

with $a_{JM} \equiv (J + \frac{1}{2})^2 - M^2$. While the 3j symbol in Eq. (5) usually is a rapidly oscillating function of M_{ν} and M_{π} , its classical approximation is smooth. Many oscillations occur except when J is close to its minimum or

maximum value, $J = |J_{\nu} - J_{\pi}|$ or $J = J_{\nu} + J_{\pi}$, respectively. The approximation (5) in the sum (4), therefore, can be expected to be reasonable in most cases, in particular in the region of physics interest where $J^2 \approx J_{\nu}^2 + J_{\pi}^2$. Since $J_{\rho} \approx j_{1\rho} + j_{2\rho}$, a classical approximation cannot be made for the first two 3j symbols in Eq. (4). From the explicit expressions for the 3j symbols one can show that the sum over M_{ν} and M_{π} can be restricted to the region around $M_{\nu} = M_{\pi} = 0$. Since the classical approximation (5) is nearly constant for small values of M_{ν} and M_{π} , the classical limit for the 3j symbols with zero projections on the z axis can be taken, to obtain

$$\sigma_0^{(0)} \approx \sigma_1^{(0)} \approx \frac{(2J_\nu + 1)(2J_\pi + 1)}{4\pi(2j_{1\nu} + 1)(2j_{1\pi} + 1)A},\tag{7}$$

where $A \equiv A_{000}^{J_{\nu}J_{\pi}J}$ is the area of a triangle with sides of lengths $J_{\nu} + \frac{1}{2}$, $J_{\pi} + \frac{1}{2}$, and $J + \frac{1}{2}$ [20]. We may alterna-

tively express this sum in terms of the shears angle,

$$\theta_{\nu\pi} = \arccos \frac{J(J+1) - J_{\nu}(J_{\nu}+1) - J_{\pi}(J_{\pi}+1)}{2\sqrt{J_{\nu}(J_{\nu}+1)J_{\pi}(J_{\pi}+1)}}, \quad (8)$$

leading to

$$\sigma_0^{(0)} \approx \sigma_1^{(0)} \approx \frac{2}{\pi (2j_{1\nu} + 1)(2j_{1\pi} + 1)\sin\theta_{\nu\pi}}.$$
 (9)

A similar derivation yields the classical approximation

$$\sigma_0^{(1)} \approx -(-)^{j_\nu + j_\pi} \frac{2}{\pi (2j_{1\nu} + 1)(2j_{1\pi} + 1)\tan\theta_{\nu\pi}}.$$
 (10)

Introducing the preceding approximations into the expression for the shears matrix element (1), we obtain

$$\langle NP^{-1}; J | V_{\nu\pi}^{\text{SDI}} | NP^{-1}; J \rangle \approx \frac{s_2}{2\pi \sin \theta_{\nu\pi}} + \frac{t_2}{2\pi \tan \theta_{\nu\pi}}, \tag{11}$$

where

$$s_{2} = 4(3a_{0} + a_{1}), \qquad t_{2} = \varphi(a_{0} - a_{1}),$$

$$\varphi = \mathcal{P}(-)^{\ell_{1\nu} + j_{1\nu} + \ell_{1\pi} + j_{1\pi}}.$$
(12)

The classical limit of the shears matrix element for the SDI does not depend on the individual single-particle angular momenta but only on the shears angle, which is defined by the angular momenta J_{ν} and J_{π} of the blades and the total angular momentum J.

In Fig. 1 the exact shears matrix elements of the SDI are compared with their classical approximation for the neutron and proton angular momenta of the blades $J_{\nu} = J_{\pi} = 20$. The approximation is good for the stretched case, $J_{\rho} = j_{1\rho} + j_{2\rho}$, but deteriorates rapidly as J_{ρ} diminishes. However, in the region of interest, where the two angular momenta J_{ν} and J_{π} are close to orthogonal, $J^2 \approx J_{\nu}^2 + J_{\pi}^2$, the classical approximation is good, also for $J_{\rho} = j_{1\rho} + j_{2\rho} - 1$, and the geometric picture underlying the shears mechanism remains valid.

This analysis also reveals the limits of the validity of this geometric picture, as is illustrated in Fig. 2 which shows the shears matrix element of the SDI for the neutron and proton angular momenta $J_{\nu} = J_{\pi} = 12$. In one case these arise from aligned single-particle angular momenta $(j_{1\rho} = \frac{11}{2} \text{ and } j_{2\rho} = \frac{13}{2})$ and the classical approximation is seen to be reasonable. In the second case the single-particle angular momenta are larger $(j_{1\rho} = j_{2\rho} = \frac{21}{2})$ and they are not aligned $(J_{\rho} = j_{1\rho} + j_{2\rho} - 9)$, leading to a breakdown of the shears interpretation. The alignment of the particles in high-*j* orbits, introduced here by hand, is in a more realistic shell-model calculation due to their interaction with particles in low-*j* orbits [9].

The classical expression (11) is reminiscent of the interpretation of nuclear matrix elements in terms of the angle between the vectors of the single-particle angular momenta (see, *e.g.*, Schiffer and True [21]). In fact, it can be shown that the classical limit of the 1p-1h matrix element $\langle j_{\nu}j_{\pi}^{-1}; J|V_{\nu\pi}^{\text{SDI}}|j_{\nu}j_{\pi}^{-1}; J\rangle$ leads to the same



FIG. 1: The exact expression (1) for the 2p-2h shears matrix element of the SDI (dots) compared with its classical approximation (11) (lines) for neutron and proton angular momenta $J_{\nu} = J_{\pi} = 20$. The single-particle angular momenta are $j_{1\rho} = \frac{19}{2}$ and $j_{2\rho} = \frac{21}{2}$ (top), and $j_{1\rho} = j_{2\rho} = \frac{21}{2}$ (bottom). Results are shown for three choices of the ratio a_0/a_1 . The matrix element is in units a_1 .



FIG. 2: Same as Fig. 1 for neutron and proton angular momenta $J_{\nu} = J_{\pi} = 12$ and single-particle angular momenta $j_{1\rho} = \frac{11}{2}$ and $j_{2\rho} = \frac{13}{2}$ (top), and $j_{1\rho} = j_{2\rho} = \frac{21}{2}$ (bottom).



FIG. 3: Experimental (points) and calculated (lines) B(M1) values for band 1 in ¹⁹⁹Pb as a function of twice the angular momentum J. The red line is the exact expression and the blue line is its classical limit (13).

dependence on the angle $\theta_{\nu\pi}$ as in Eq. (11) but with coefficients s_1 and t_1 that depend differently on the strengths a_T of the interaction.

The present results make contact with the semiclassical analysis [5, 6] in terms of an interaction $V_0 + V_2 P_2(\cos \theta_{\nu\pi})$, assumed to exist between the blades of the shears bands. In line with the intuitive picture one has of the shears mechanism, this interaction necessarily implies a shears-band head with $\cos \theta_{\nu\pi}^0 \approx 0$ or, alternatively, a minimum energy for $J^2 \approx J_{\nu}^2 + J_{\pi}^2$ when the angular momentum vectors \bar{J}_{ν} and \bar{J}_{π} are orthogonal. Our analysis shows that this is not generally valid since a minimum energy is obtained from Eq. (11) for $\cos \theta_{\nu\pi}^0 \approx -t_2/s_2 = \varphi(a_1 - a_0)/4(3a_0 + a_1)$. Therefore, if the isoscalar and isovector interaction strengths are different, a minimum energy is found for a *non-orthogonal* configuration.

Shears bands are characterized by strong M1 transitions that decrease with increasing angular momentum J. For a general configuration $|NP^{-1}; J\rangle$, where $|N\rangle$ is an *m*-particle neutron and $|P^{-1}\rangle$ an *m'*-hole proton configuration with angular momenta J_{ν} and J_{π} , respectively,

$$B(M1; J \to J - 1) \\\approx \frac{3}{4\pi} (g_{\nu} - g_{\pi})^2 \frac{(2J_{\nu} + 1)^2 (2J_{\pi} + 1)^2}{16J(2J + 1)} \sin^2 \theta_{\nu\pi}, (13)$$

where g_{ν} and g_{π} are the g factors of the neutron and proton configurations $|N\rangle$ and $|P^{-1}\rangle$, respectively. This expression can be tested in ¹⁹⁹Pb where lifetimes of some shears-band levels have been measured [23]. In particular, the states in band 1 with $\frac{43}{2} < J < \frac{55}{2}$ have the suggested [24] configuration $\nu(1i_{13/2}^{-3})_{33/2} \times \pi(1h_{9/2}1i_{13/2})_{11}$, from where the g factors can be obtained, $g_{\nu} = -0.29 \ \mu_{\rm N}$ and $g_{\pi} = 1.03 \ \mu_{\rm N}$. Application of Eq. (13) with $J_{\nu} = \frac{33}{2}$ and $J_{\pi} = 11$ leads to the result shown in Fig. 3 (in blue), which is seen to be close to the exact result (in red). In the spin region $\frac{47}{2} \leq J \leq \frac{53}{2}$, where the above configuration is thought to apply, agreement is obtained.

The data on M1 transitions indicate that fixed neutron and proton configurations do not apply to an entire shears band but only to part of it. For this reason it will be difficult to use energy formulas like Eq. (11) with constant coefficients s_2 and t_2 for an entire band. The present analysis suggests however that, under certain conditions of angular-momentum alignment, the generic form of the expression (11) is approximately valid with coefficients s_i and t_i depending on the structure of the neutron and proton configurations that apply to certain ranges of the total angular momentum J. This problem is currently under study.

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