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► To cite this version:

Guy Royer, Christelle Gautier. Coefficients and terms of the liquid drop model and mass formula. Physical Review C, 2006, 73, pp.067302. 10.1103/PhysRevC.73.067302. in2p3-00089830

HAL Id: in2p3-00089830 https://in2p3.hal.science/in2p3-00089830v1

Submitted on 24 Aug 2006

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On the coefficients and terms of the liquid drop model and mass formula

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(Dated: August 28, 2006)

The coefficients of different combinations of terms of the liquid drop model have been determined by a least square fitting procedure to the experimental atomic masses. The nuclear masses can also be reproduced using a Coulomb radius taking into account the increase of the ratio $R_0/A^{1/3}$ with increasing mass, the fitted surface energy coefficient remaining around 18 MeV.

PACS numbers: 21.10.Dr; 21.60.Ev; 21.60.Cs

To predict the stability of new nuclides both in the superheavy element region and the regions close to the proton and neutron drip lines continuous efforts are still needed to determine the nuclear masses and therefore the binding energies of such exotic nuclei. Within a modelling of the nucleus by a charged liquid drop, semimacroscopic models including a pairing energy have been firstly developed to reproduce the experimental nuclear masses [1, 2]. The coefficients of the Bethe-Weizsäcker mass formula have been determined once again recently To reproduce the non-smooth behaviour of the [3].masses (due to the magic number proximity, parity of the proton and neutron numbers,...) and other microscopic properties, macroscopic-microscopic approaches have been formulated, mainly the finite-range liquid drop model and the finite-range droplet model [4]. Nuclear masses have also been obtained accurately within the statistical Thomas-Fermi model with a well-chosen effective interaction [5, 6]. Microscopic Hartree-Fock selfconsistent calculations using mean-fields and Skyrme or Gogny forces and pairing correlations [7, 8] as well as relativistic mean field theories [9] have also been developed to describe these nuclear masses. Finally, nuclear mass systematics using neural networks have been undertaken recently [10].

The nuclear binding energy $B_{nucl}(A,Z)$ which is the energy necessary for separating all the nucleons constituting a nucleus is connected to the nuclear mass $M_{n.m}$ by

$$B_{nucl}(A, Z) = Zm_P + Nm_N - M_{n.m}(A, Z).$$
 (1)

This quantity may thus be easily derived from the experimental atomic masses as published in [11] since :

$$M_{n.m}(A, Z) = M_{a.m}(A, Z) - Zm_e + B_e(Z)$$
(2)

while the binding energy $B_e(Z)$ of all removed electrons is given by [12]

$$B_e(Z) = a_{el} Z^{2.39} + b_{el} Z^{5.35}, (3)$$

with
$$a_{el} = 1.44381 \times 10^{-5}$$
 MeV and $b_{el} = 1.55468 \times 10^{-12}$ MeV.

The fission, fusion, cluster and α decay potential barriers are governed by the evolution of the nuclear binding energy with deformation. It has been shown that four basic terms are sufficient to describe the main features of these barriers [13, 14, 15, 16, 17, 18] : the volume, surface, Coulomb and nuclear proximity energy terms while the introduction of the shell and pairing energy terms is needed to explain structure effects and improve quantitatively the results. Other terms have been proposed to determine accurately the binding energy and other nuclear characteristics : the curvature, A⁰, proton form factor correction, Wigner, Coulomb exchange correction,...energy terms [4].

The purpose of the present work is to determine the coefficients of different combinations of terms of the liquid drop model by a least square fitting procedure to the experimentally available atomic masses [11] and to study whether nuclear masses can also be reproduced using, for the Coulomb energy, a radius which takes into account the small decrease of the density with increasing mass and to determine the associated surface energy coefficient. The theoretical shell effects given by the Thomas-Fermi model $(7^{th}$ column of the table in [5] and [6]) have been selected since they reproduce nicely the mass decrements from fermium to Z = 112 [19]. They are based on the Strutinsky shell-correction method and given for the most stable nuclei in the appendix. The masses of the 1522 nuclei verifying the two following conditions have been used : N and Z higher than 7 and the one standard deviation uncertainty on the mass lower than 100 keV [11].

The following expansion of the nuclear binding energy has been considered

$$B_{nucl} = a_v (1 - k_v I^2) A - a_s (1 - k_s I^2) A^{2/3} - \frac{3}{5} \frac{e^2 Z^2}{R_0} (4) + E_{pair} - E_{shell} - a_k A^{1/3} - a_0 A^0 - f_p \frac{Z^2}{A} - W|I|.$$

The nuclear proximity energy term does not appear since its effect is effective only for necked shapes but not around the ground state. The first term is the volume

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energy and corresponds to the saturated exchange force and infinite nuclear matter. In this form it includes the asymmetry energy term of the Bethe-Weizsäcker mass formula via the relative neutron excess I=(N-Z)/A. The second term is the surface energy term. It takes into account the deficit of binding energy of the nucleons at the nuclear surface and corresponds to semi-infinite nuclear matter. The dependence on I is not considered in the Bethe-Weizsäcker mass formula. The third term is the Coulomb energy. It gives the loss of binding energy due to the repulsion between the protons. In the Bethe-Weizsäcker mass formula the proportionality to Z(Z-1) is assumed.

The pairing energy has been calculated using

$$\begin{split} E_{pair} &= -a_p/A^{1/2} \text{ for odd Z, odd N nuclei,} \\ & E_{pair} = 0 \text{ for odd A,} \\ E_{pair} &= a_p/A^{1/2} \text{ for even Z, even N nuclei.} \end{split}$$
 (5)

The $a_p = 11$ value has been adopted following first fits. Other more sophisticated expressions exist for the pairing energy [4, 6].

The sign for the shell energy term comes from the adopted definition in [5]. It gives a contribution of 12.84 MeV to the binding energy for ²⁰⁸Pb for example. The curvature energy $a_k A^{1/3}$ is a correction to the surface energy appearing when the surface energy is considered as a function of local properties of the surface and consequently depends on the mean local curvature. The $a_0 A^0$ term appears when the surface term of the liquid drop model is extended to include higher order terms in $A^{-1/3}$ and I. The last but one term is a proton formfactor correction to the Coulomb energy which takes into account the finite size of the protons. The last term is the Wigner energy [4, 20] which appears in the counting of identical pairs in a nucleus, furthermore it is clearly called for by the experimental masses.

In Table 1 the improvement of the experimental data reproduction when additional terms are added to the three basic volume, surface and Coulomb energy terms is displayed when the nuclear radius is calculated by the formula $R_0=r_0A^{1/3}$.

The root-mean-square deviation, defined by :

$$\sigma^2 = \frac{\Sigma \left[M_{Th} - M_{Exp} \right]^2}{n} \tag{6}$$

has been used to compare the efficiency of these different selected sets of terms.

To follow the non smooth variation of the nuclear masses with A and Z the introduction of the shell energy is obviously needed as well as that of the pairing term though its effect is smaller. The curvature term and the constant term taken alone do not allow to better fit the experimental masses while the proton form factor correction to the Coulomb energy and the Wigner term have separately a strong effect in the decrease of σ . When both these two last contributions to the binding energy are taken into account $\sigma = 0.58$ MeV which

is a very satisfactory value [4, 8, 20]. The addition to the proton form factor and Wigner energy terms of the curvature energy or constant terms taken separately or together does not allow to improve σ . Furthermore, a progressive convergence of a_k and a_0 is not obtained and strange surface energy coefficients appear. Due to this strong variation and lack of stability of the curvature and constant coefficient values it seems preferable to neglect these terms since the accuracy is already correct without them. Disregarding the last line a good stability of the volume a_v and asymmetry volume k_v constants is observed. The variation of the surface coefficient is larger but a_s reaches a maximum of only 18 MeV. As it is well known the surface asymmetry coefficient \mathbf{k}_s is less easy to precise. Invariably r_0 has a value of around 1.22 fm within this approach.

For the Bethe-Weizsäcker formula the fitting procedure leads to

$$B_{nucl}(A,Z) = 15.7827A - 17.9042A^{2/3} \quad (7)$$
$$-0.72404 \frac{Z(Z-1)}{A^{1/3}} - 23.7193I^2A + E_{pair} - E_{shell}$$

with $\sigma = 1.17$ MeV. That leads to $r_0 = 1.193$ fm and $k_v = 1.505$. The non dependence of the surface energy term on the relative neutron excess I explains the σ value.

The formula $R_0=r_0A^{1/3}$ does not reproduce the small decrease of the density with increasing mass [20]. In previous works [13, 14, 15, 16, 17, 18] the formula

$$R_0 = 1.28A^{1/3} - 0.76 + 0.8A^{-1/3} \tag{8}$$

proposed in Ref. [21] for the effective sharp radius has been retained to describe the main properties of the fusion, fission, cluster and α emission potential barriers in the quasi-molecular shape path. It leads for example to $r_0=1.13$ fm for ⁴⁸Ca and $r_0=1.18$ fm for ²⁴⁸Cm. The fit of the nuclear binding energy by the expression (6) is reconsidered in the table 2 in calculating the Coulomb energy by the formula $\frac{3}{5} \frac{e^2 Z^2}{1.28 A^{1/3} - 0.76 + 0.8 A^{-1/3}}$ without adjustable parameter. The behaviour of the different combinations of terms is about the same as in table 1. It seems also preferable to disregard the curvature and constant contributions. Then σ takes the value 0.60 MeV to be compared to 0.58 MeV in the first table when the Coulomb energy contains an additional adjustable parameter.

The figure shows that the difference between the theoretical and experimental masses never exceeds 2.25 MeV and is less than 1.15 MeV when A is higher than 100. In the Generalized Liquid Drop Model [13, 14] the selected values are $a_v=15.494$ MeV, $a_s=17.9439$ MeV, $k_v=1.8$ and $k_s=2.6$. They are close to the ones given $\sigma=0.60$ MeV in table 2.

As a conclusion, the most important result is that it is possible to reproduce the nuclear masses in taken a realistic formula for the effective sharp radius given $R_0/A^{1/3}=1.1$ fm for the lightest nuclei and 1.18 fm for

TABLE I: Dependence of the energy coefficient values (in MeV or fm) on the selected term set including or not the pairing and theoretical shell energies and root mean square deviation. The Coulomb energy is determined by $a_c \frac{Z^2}{A^{1/3}}$ with $a_c = 3e^2/5r_0$.

a_v	k_v	a_s	k_s	r_0	a_k	a_0	f_p	W	Pairing	Shell	σ
15.7335	1.6949	17.8048	1.0884	1.2181	-	-	-	-	n	n	2.92
15.6335	1.6810	17.2795	0.8840	1.2208	-	-	-	-	n	У	1.26
15.6562	1.6803	17.3492	0.8710	1.2181	-	-	-	-	У	У	0.97
15.2374	1.6708	15.4913	0.9223	1.2531	-	7.3742	-	-	У	У	0.92
14.8948	1.6686	12.8138	1.0148	1.2721	7.6659	-	-	-	У	У	0.88
15.4443	1.9125	16.5842	2.4281	1.2444	-	-	-	44.2135	У	У	0.70
15.5424	1.7013	18.0625	1.3175	1.2046	-	-	-1.40745	-	У	У	0.68
15.4496	1.8376	17.3525	2.0990	1.2249	-	-	-0.93794	27.2843	у	У	0.584
15.5518	1.8452	18.015	2.0910	1.2176	-1.1207	-	-0.97833	28.4963	У	У	0.582
15.5293	1.8462	17.7376	2.1163	1.2182	-	-1.5576	-0.96851	28.6061	У	У	0.581
14.8497	1.8373	11.2996	2.7852	1.2505	20.9967	-25.7261	- 0.6862	26.4072	у	У	0.57

TABLE II: Dependence of the energy coefficient values (in MeV) on the selected term set including or not the pairing and shell energies and the corresponding root mean square deviations. The Coulomb energy coefficient is not adjusted and is determined by $\frac{3}{5} \frac{e^2 Z^2}{1.28 A^{1/3} - 0.76 + 0.8 A^{-1/3}}$.

a_v	k_v	a_s	k_s	a_k	a_0	f_p	W	Pairing	Shell	σ
15.9622	1.7397	18.0108	1.0627	-	-	-	-	n	n	3.12
15.8809	1.7201	17.5366	0.8234	-	-	-	-	n	У	1.56
15.8846	1.7256	17.5547	0.8475	-	-	-	-	У	У	1.32
15.8533	1.8937	17.2793	1.9924	-	-	-	44.4714	У	У	1.04
15.5887	1.8011	18.194	1.7271	-	-	-1.98718	-	У	У	0.83
15.6089	1.9136	17.9021	2.4111	-	-	-1.69912	32.1647	У	У	0.599
15.5833	1.8988	17.726	2.3495	0.433	-	-1.73074	29.8599	У	У	0.598
15.5996	1.9061	17.8631	2.3757	-	0.3146	-1.71583	31.0077	У	У	0.599
15.3737	1.8892	14.9364	2.5745	12.418	-16.7906	-1.71391	27.8208	У	У	0.58



FIG. 1: Difference (in MeV) between the theoretical and experimental masses for the 1522 nuclei as a function of the mass number.

the heaviest ones while the surface energy coefficient remains around 18 MeV and the surface-asymmetry coefficient around 2.5. Besides the values of the volume, surface and Coulomb energy coefficients the accuracy of the fitting depends also strongly on the selected shell and pairing energies as well as on the proton form factor and Wigner energy terms.

APPENDIX A: TABLE III

TABLE III: Theoretical shell energy (in MeV) extracted from [5] (7^{th} column) at the ground state of nuclei for which the half-life is higher than 1 ky.

10 P	$^{11} B$	12C	^{13}C	^{14}C	14 N	15 N	¹⁶ O	170	180	19 E	^{20}Nc	^{21}Nc	$^{22}N_{\odot}$
2.36	0.74	-0.69	-1 03	-0.56	-1.33	-0.87	-0.45	1 19	13	2.76	2.81	2.82	2.19
^{23}Na	^{24}Mq	^{25}Mq	^{26}Mq	^{26}Al	^{27}Al	^{28}Si	^{29}Si	${}^{30}Si$	^{31}P	^{32}S	$\frac{2.01}{33}S$	^{34}S	$\frac{2.10}{^{36}S}$
2.22	1.64°	1.77°	0.64°	1.89	0.79	-0.26	-0.25	0.22	0.22	0.66	0.86	1.13	1.22
^{35}Cl	^{36}Cl	^{37}Cl	^{36}Ar	^{38}Ar	^{40}Ar	^{39}K	${}^{40}K$	${}^{41}K$	^{40}Ca	^{41}Ca	^{42}Ca	^{43}Ca	^{44}Ca
1.32	1.48	1.40	1.57	1.64	2.45	1.79	2.58	2.58	1.71	2.49	2.49	2.16	1.7
^{46}Ca	^{48}Ca	^{45}Sc	${}^{46}Ti$	^{47}Ti	${}^{48}Ti$	${}^{49}Ti$	^{50}Ti	${}^{50}V$	${}^{51}V$	^{50}Cr	^{52}Cr	^{53}Cr	^{54}Cr
0.69	-0.82	2.43	2.44	1.95	1.44	0.81	-0.05	0.54	-0.31	0.74	-0.69	-0.38	0.74
^{53}Mn	^{55}Mn	${}^{54}Fe$	${}^{56}Fe$	${}^{57}Fe$	^{58}Fe	${}^{60}Fe$	^{59}Co	^{58}Ni	^{59}Ni	^{60}Ni	^{61}Ni	^{62}Ni	^{64}Ni
-1.11	0.68	-1.54	0.05	0.72	1.22	2.07	0.77	-1.58	-0.68	-0.16	0.59	1.1	1.63
^{03}Cu	^{05}Cu	^{04}Zn	^{00}Zn	$^{\circ}Zn$	^{00}Zn	^{10}Zn	^{09}Ga	Ga	1º Ge	'*Ge	1º Ge	'⁴Ge	¹⁰ Ge
1.80	2.33	2.53 76	2.89	$\frac{3.16}{78 c}$	2.99	2.94 80 a	$\frac{3.79}{82 c}$	3.71 79 D	4.13 81 D	4.08 80 L	4.19 81 K	3.82 82 1/	2.53 83 1/
AS	- Se	1 08	··· Se	~ Se	~ Se	** Se	Se	$^{\circ}Br$	$^{\circ-}Br$	$^{\circ\circ}Kr$	$^{\circ}Kr$	$^{\circ-}Kr$	
$\frac{4.08}{84} K_m$	$\frac{4.42}{86}$ Km	$\frac{4.08}{85} Dh$	$\frac{4.00}{87}$ Dh	3.21 $86 C_m$	2.01 $87 C_{m}$	1.09 $88 G_m$	0.38 ^{89}V	$\frac{4.07}{90}$	$\frac{2.28}{91}$ Zm	$\frac{4.59}{92}$ 7 m	3.11 937	$\frac{2.14}{947m}$	96 7
0.96	-0.40	1 1 3	-0.35	0.79	0.05	-0.97	_1 10	_1.63	-0.47	0.46	2T 1.53	27 254	21 3 / 0
^{92}Nh	$^{+0.40}$ ^{93}Nb	^{94}Nb	$^{-0.30}_{92}Mo$	^{93}Mo	^{94}Mo	$^{-0.51}_{95}Mo$	^{96}Mo	$^{-1.05}$ ^{97}Mo	$^{-0.41}_{98}Mo$	^{100}Mo	^{97}Tc	$^{2.04}_{98}Tc$	^{99}Tc
-0.57	0.44	1.51	-2.12	-1.07	-0.12	0.97	1.79	2.46	2.98	3.62	1.26	2.05	2.64
${}^{96}Ru$	^{98}Ru	^{99}Ru	^{100}Ru	^{101}Ru	^{102}Ru	^{104}Ru	^{103}Rh	^{102}Pd	^{104}Pd	^{105}Pd	^{106}Pd	^{107}Pd	^{108}Pd
-1.11	0.57	1.36	2.00	2.54	2.98	3.49	2.44	0.63	1.83	2.39	2.80	3.08	3.34
^{110}Pd	^{107}Ag	^{109}Ag	^{106}Cd	^{108}Cd	^{110}Cd	^{111}Cd	^{112}Cd	^{113}Cd	^{114}Cd	^{116}Cd	^{113}In	^{115}In	^{112}Sn
3.42	2.20	2.91	0.31	1.35	2.11	2.42	2.52	2.61	2.50	2.26	1.83	1.97	0.37
^{114}Sn	^{115}Sn	^{116}Sn	^{117}Sn	^{118}Sn	^{119}Sn	^{120}Sn	^{122}Sn	^{124}Sn	^{126}Sn	^{121}Sb	^{123}Sb	^{120}Te	^{122}Te
0.81	1.03	0.94	0.96	0.75	0.70	0.19	-0.99	-2.51	-4.36	0.76	-0.16	2.08	1.55
^{123}Te	^{124}Te	¹²⁵ Te	^{120}Te	^{120}Te	^{130}Te	12' I	¹²⁹]	¹²⁰ Xe	¹²⁹ Xe	¹³⁰ Xe	^{131}Xe	^{132}Xe	¹³⁴ Xe
1.30 136 yz	0.66	0.25	-0.62	-2.46	-4.74	0.35 136 p	-1.29 137 D	1.01 138 D	0.48	-0.31	-1.11 139 r	-2.36	-4.92
Xe 7.0	1 98	200	-3-Ba	0 EE	1 45	2 01	Ba	500 Ba	<i>La</i>	227	4 50	0.70	1 57
-1.2	$^{-1.26}_{142}C_{c}$	-5.90 $141 D_m$	0.95 142 Md	-0.55 143 M.J	-1.40 144 M.d	$^{-5.01}_{145 Md}$	-4.10 146 Md	-3.29 148 M.J	-2.22 150 M.d	-3.37 144 Gm	-4.50 146 c_m	$147 G_{m}$	-1.57 148 Cm
-3.86	-2.06	-3.26	_2 88	_2 14	-1 04	0.10	0.56	0.85	0.54	_2 28	-0.41	0.67	112
$^{-9.00}_{149}Sm$	$^{-2.00}_{150}Sm$	$^{-5.20}_{152}Sm$	$^{-2.00}_{154}Sm$	$^{-2.14}_{151}Eu$	$^{-1.04}_{153}Eu$	^{150}Gd	^{152}Gd	^{154}Gd	^{155}Gd	$^{-2.20}_{156}Gd$	^{157}Gd	^{158}Gd	$^{1.12}_{160}Gd$
1.22	1.31	0.90	0.38	1.39	1.02	1.30	1.59	1.33	1.05	0.89	0.62	0.56	0.21
^{159}Tb	^{154}Dy	^{156}Dy	^{158}Dy	^{160}Dy	^{161}Dy	^{162}Dy	^{163}Dy	^{164}Dy	^{165}Dy	^{163}Ho	^{165}Ho	^{162}Er	^{164}Er
0.64	1.63	1.56	1.24	0.92	0.64	0.47	0.16	-0.06	-0.41	0.46	-0.12	1.20	0.70
^{166}Er	^{167}Er	^{168}Er	^{170}Er	^{169}Tm	^{168}Yb	^{170}Yb	^{171}Yb	^{172}Yb	^{173}Yb	^{174}Yb	^{176}Yb	^{175}Lu	^{176}Lu
0.07	-0.37	-0.54	-1.08	-0.60	0.32	-0.34	-0.76	-0.94	-1.32	-1.30	-1.74	-1.23	-1.62
^{174}Hf	^{176}Hf	^{177}Hf	^{178}Hf	^{179}Hf	^{180}Hf	^{182}Hf	^{181}Ta	^{180}W	^{182}W	^{183}W	^{184}W	^{186}W	^{185}Re
-0.38	-0.90	-1.33	-1.53	-1.97	-1.99	-2.16	-2.02	-1.21	-1.71	-2.00	-2.02	-2.38	-2.19
$^{10'}Re$	^{104}Os	^{100}Os	^{10}Os	^{100}Os	^{109}Os	^{190}Os	^{192}Os	¹⁹¹ <i>Ir</i>	¹⁹³ <i>Ir</i>	¹⁹⁰ <i>Pt</i>	^{192}Pt	^{194}Pt	^{195}Pt
-2.48	-1.61 198 ית	-1.88 197 4	-2.16 196 II	-2.08 198 II	-2.43 199 II	-2.47 200 II	-3.50 201 m	-2.54 202 II	-3.62 204 11	-0.97	-2.01	-3.31 202 ית	-4.04
$^{}Pt$	$^{}Pt$	Au 5 56	Hg 451	<i>Hg</i>	Hg 6 75	Hg 7 59	Hg 0 27	<i>Hg</i>	Hg 10.60	0.07	11 59	Pb	10.02
-4.80 205 Ph	$^{-0.11}_{206} Ph$	$^{-0.00}_{207 Ph}$	$^{-4.01}_{208 Dh}$	$^{-0.99}_{208}$ B ²	$^{-0.70}_{209} B_{i}$	-1.02 226 Bc	-0.31 ²²⁹ Th	$^{-9.11}_{230}Th$	$^{-10.09}_{232}Th$	-9.97 ^{231}Pc	^{233}U	$^{-0.22}_{234}$	$^{-10.02}_{235}$
-11.00	-11.82	-12.68	-12.84	-1170	-11.95	-0.30	-0.52	-0.43	-0.60	-0 79	-1 27	-1 23	-1 46
^{236}U	^{238}U	^{236}Nn	237 Nn	^{239}Pu	^{240}Pu	^{242}Pu	^{244}Pn	^{243}Am	^{245}Cm	^{246}Cm	^{247}Cm	^{248}Cm	^{247}Bk
-1.30	-1.27	-1.85	-1.74	-2.12	-1.95	-1.99	-2.08	-2.44	-3.05	-2.96	-3.17	-3.00	-3.46

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