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**Search for a non-minimal Higgs boson
produced in the reaction $e^+e^- \rightarrow hZ^*$**

The ALEPH Collaboration*)

Abstract

A data sample corresponding to 1.23 million hadronic Z decays collected by the ALEPH detector at LEP has been searched for signals of the production of a non-minimal CP-even Higgs boson h in the reaction $e^+e^- \rightarrow hZ^*$. The h decay modes considered were: those of the minimal standard model Higgs boson, with modified branching ratios; decays into a pair of CP-odd Higgs bosons A; and decays into invisible final states. Only one event was found, a very acoplanar e^+e^- pair which could originate from the standard model background process $e^+e^- \rightarrow e^+e^-\nu\bar{\nu}$. Upper limits for the cross-section of the reaction $e^+e^- \rightarrow hZ^*$ have been derived as a function of m_h , the mass of the Higgs boson h. In the case of invisible decays, the 95% CL lower limit on m_h is 65 GeV/ c^2 for a production cross-section equal to that of a minimal standard model Higgs boson. When combined with previous ALEPH results on the reaction $e^+e^- \rightarrow hA$, these cross-section upper limits exclude a domain in the (m_h, m_A) plane of the MSSM such that, if invisible h and A decays can be neglected, 95% CL lower limits of 44 and 21 GeV/ c^2 result for m_h and m_A , respectively, independent of the other parameters of the model.

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1. Introduction

The searches for the Higgs boson of the minimal standard model (MSM) produced in the bremsstrahlung process $e^+e^- \rightarrow HZ^*$ can in principle be applied to a CP-even Higgs boson h of any non-minimal model, taking into account a model dependent factor, denoted ξ^2 in the following, by which the production rate is reduced.

In this letter, only those non-minimal models [1] are considered which contain Higgs fields in $SU(2)_L$ representations not larger than doublets. In this case, the tree-level value of ρ [2] automatically remains equal to unity, as required by precision electroweak measurements. In addition, in order to avoid flavour changing neutral currents, one of the Higgs doublets, say the first one, is required to couple to down-type quarks and to charged leptons only while the second one couples to up-type quarks only. The ratio v_2/v_1 of the vacuum expectation values developed by the neutral components of the two Higgs doublets is denoted $\tan \beta$. Finally, additional Higgs field singlets may or may not be present.

In these models, the couplings of the Higgs boson h to down-type quarks and to charged leptons remain in the same ratios as in the MSM. In particular, this is the case for the ratio of the hbb and $h\tau\tau$ couplings. On the other hand, the ratios of the hcc to the hbb or $h\tau\tau$ couplings can be very different from their MSM values.

A well known example of such non-minimal models is the minimal supersymmetric extension of the standard model (MSSM) [1] which does not contain additional singlets and in which ξ^2 is equal to $\sin^2(\beta - \alpha)$, where α is the mixing angle in the CP-even Higgs sector. In the MSSM, it is commonly assumed that $\tan \beta > 1$, in which case the couplings of h to down-type quarks (such as the b-quark) and to charged leptons (such as the τ) are enhanced with respect to those of the MSM Higgs boson, and the couplings to up-type quarks (such as the c-quark) are reduced. The analyses presented in this letter are conducted in a framework broader than the MSSM, but the implications for this model of the results obtained are also detailed in the end.

The results of the MSM Higgs boson searches can be directly used in the context of a non-minimal model provided that the detection efficiencies are identical in the two cases. This, however, is likely not to be true if the Higgs boson decay branching ratios and, even more so, if the decay channels themselves are different. The selection criteria used by ALEPH in the search for the standard model Higgs boson are described in detail in Refs. 3 and 4.

With these criteria, there are a few situations in which detection efficiency differences can affect the results in a significant way:

- if, although the decay channels are the same, the branching ratios are modified in such a way that the various final state topologies contribute differently;
- if the decay channel $h \rightarrow AA$ is kinematically allowed (A is a CP-odd neutral Higgs boson which is not present in the MSM);
- if other decay channels not existing in the MSM are available, in particular invisible decay modes [5,6].

In the first of these instances, the selection efficiencies determined in the MSM case for every decay channel [3,4] can simply be reweighted in the most conservative way in order to take into account any possible differences in the decay branching ratios.

Dedicated searches were designed and applied to the data collected in 1989 and 1990 [3], taking into account the specific features of the $h \rightarrow AA$ channel [7]. The search criteria have been extended to be sensitive to the decays of the A boson into final states containing only neutral particles. The case of a very light A ($m_A < 2m_\mu$), already investigated in detail and excluded in a previous publication [8] within the MSSM framework for any m_h and for any $\tan\beta > 1$, is no longer considered here.

If other new decay modes are available, the most dramatic changes arise when the Higgs boson can decay invisibly. This may happen, for instance, in R-parity conserving supersymmetric models when the lightest neutralino χ is light enough for the decay $h \rightarrow \chi\chi$ to be allowed (χ is commonly expected to be the lightest supersymmetric particle, and therefore invisible). The search for such an invisible Higgs boson has now been performed for the first time.

The data sample used to obtain the results presented in the following corresponds to 1.23 million hadronic Z decays collected by the ALEPH detector at LEP from 1989 to 1992. A thorough description of the detector can be found in Ref. 9, and a brief account in Ref. 4.

In order to assess the selectivity of the various searches described in the following, large Monte Carlo samples of all standard model background processes have been used, in particular: 1.4 million $Z \rightarrow q\bar{q}$ events; 100 000 $Z \rightarrow \tau^+\tau^-$ events, corresponding to 1.6 times the data statistics; 20 000 events from the two-photon process $\gamma\gamma \rightarrow \tau^+\tau^-$ and 10 000 from $\gamma\gamma \rightarrow c\bar{c}$, corresponding to 1.8 and 1.4 times the recorded integrated luminosity, respectively. In addition, smaller simulated event samples, but all corresponding to at least twice the data statistics, have been analysed for the various processes $e^+e^- \rightarrow l^+l^-\bar{f}\bar{f}$, with $\bar{f}\bar{f} = l^+l^-$ or $q\bar{q}$. The search efficiencies for the reaction $e^+e^- \rightarrow hZ^*$ have been determined using Monte Carlo samples produced with a minimal standard model Higgs boson generator, modified to accommodate non-standard Higgs decays.

2. Results valid when no new decay channels contribute

For $m_h > 2m_b$, the configurations considered are [4] ($h \rightarrow \text{hadrons}$)($Z^* \rightarrow \nu\bar{\nu}$) and, if $m_h > 40 \text{ GeV}/c^2$, ($h \rightarrow \text{hadrons}$)($Z^* \rightarrow e^+e^-$ or $\mu^+\mu^-$). With the search criteria described in detail in Ref. 4, no candidates were found in the full data sample, leading to a mass lower limit of $58.4 \text{ GeV}/c^2$ for the MSM Higgs boson. For a non-minimal Higgs boson, the search efficiency with respect to the MSM case is essentially controlled by the value of the branching ratio of $h \rightarrow \text{hadrons}$, as compared to that of $h \rightarrow \tau^+\tau^-$. In the models considered here, this hadronic decay branching ratio reaches its minimum value when the hcc coupling vanishes, in which case it is only 1% smaller than in the MSM. The efficiency determined in the MSM Higgs boson search, displayed in Table 1 of Ref. 4, has been conservatively reduced by this amount.

For the mass range $2m_\mu < m_h < 2m_b$, only the $Z^* \rightarrow \nu\bar{\nu}$ decay is considered [3]. The relevant searches, *i.e.* those for acoplanar lepton pairs and for monojets, are described in detail in Section 4. They require, in particular, a charged particle multiplicity of at least two. One candidate event has been found, an acoplanar e^+e^- pair. The following mass ranges can be distinguished.

- $2m_\tau < m_h < 2m_b$

The search efficiency is lower for $h \rightarrow \tau^+\tau^-$ than for $h \rightarrow \text{hadrons}$. Therefore, the results are derived assuming that h mainly decays into $\tau^+\tau^-$. The resulting efficiency is 73% of that applying in the MSM case. Since the selected acoplanar e^+e^- pair mentioned above may result from a $\tau^+\tau^-$ final state, it is kept as a candidate in this mass range.

- $2m_\pi < m_h < 2m_\tau$

The detection efficiency is lowest when the fraction of final states containing no charged particles is largest. Given the decay channels allowed for a CP-even Higgs boson in this mass range [10], the worst configuration is reached when h decays into $\eta\eta$, in which case half of the final states contain only neutral particles. Conservatively, the results are derived assuming that same fraction to hold over the whole mass range, except for $m_h < 2m_K$ where only $h \rightarrow \pi\pi$ is considered, with a $\pi^0\pi^0$ fraction of one third. Here, the e^+e^- pair is not taken as a candidate because the branching ratio of $h \rightarrow e^+e^-$ is always negligible in this mass range.

- $2m_\mu < m_h < 2m_\pi$

The only relevant decay channel is $h \rightarrow \mu^+\mu^-$, and the search efficiency determined in the MSM case applies without modification. No events have been found.

For $m_h < 2m_\mu$, the lifetime of the Higgs boson can no longer be ignored. If the lifetime is very large, the search for an invisible Higgs boson reported in Section 4 applies and, anticipating the results obtained therein, the 95% CL upper limit on ξ^2 is found to be $2.3 \cdot 10^{-3}$. For sufficiently small lifetimes, the search for acoplanar lepton pairs described in Section 4 could be used for the configuration ($h \rightarrow e^+e^-$)($Z^* \rightarrow \nu\bar{\nu}$). However, since the competing $h \rightarrow \gamma\gamma$ decay mode proceeds *via* loop diagrams, its rate is sensitive to the

details of the model. Therefore, no general statement can be made for this mass range without a dedicated analysis.

The 95% CL upper limit on ξ^2 resulting from these studies is displayed in Fig. 1 as a function of m_h . For $\xi^2 = 1$, the lower limit on m_h is 58.4 GeV/ c^2 .

3. Results valid when the $h \rightarrow AA$ decay channel is dominant

Here, the value of the A mass plays an important rôle. If $m_A \gtrsim 2m_b$, the final state resulting from $h \rightarrow AA$ does not show any features, for instance in the charged multiplicity, which could lower the selection efficiency with respect to the MSM case. However, for the mass ranges $2m_\tau < m_A \lesssim 2m_b$ (in which $A \rightarrow \tau^+\tau^-$ may dominate over $A \rightarrow c\bar{c}$) and $m_A < 2m_\tau$, the final state resulting from $h \rightarrow AA$ may exhibit a charged multiplicity which is too low compared to the requirements [4] applied in the search for a similar mass MSM Higgs boson.

Specific searches have been designed previously [3] for the configurations ($h \rightarrow AA$) ($Z^* \rightarrow e^+e^-$ or $\mu^+\mu^-$ or $\nu\bar{\nu}$), with the resulting A bosons decaying into low mass and low charged multiplicity systems. The search criteria have been extended in order to be sensitive to final states in which one of the two A bosons decays into a system containing only neutral particles, which may occasionally happen in the case of an A boson mass below the $\tau^+\tau^-$ and $c\bar{c}$ thresholds (*e.g.* if $A \rightarrow \eta\eta\eta$ with $\eta \rightarrow \gamma\gamma$ or $3\pi^0$).

The selection criteria for ($h \rightarrow AA$) ($Z^* \rightarrow \nu\bar{\nu}$) are listed below.

The total charged multiplicity must be 2, 4 or 6, including tracks possibly coming from long lived neutral particle (V^0) decays, and the total electric charge must be zero. Larger charged multiplicities are covered by the MSM Higgs boson search in the acoplanar jet topology [4]. In order to avoid energy losses in the very forward and backward directions, it is required that no energy be detected within 12° of the beam axis, and that no track be reconstructed with a polar angle θ with respect to that axis such that $|\cos\theta| > 0.95$. Events resulting from two photon processes are largely eliminated by the requirement that the total momentum transverse to the beam direction exceed 5% of the centre-of-mass energy.

The remaining events are divided into two hemispheres by a plane perpendicular to the thrust axis. Each hemisphere must contain no more than 4 tracks with a total electric charge equal to zero. In each hemisphere, the total energy must exceed 2 GeV and, in order to ensure that the final state is well contained in the detector, the direction of the total momentum is required to have a polar angle θ such that $|\cos\theta| < 0.9$. As in the search for acoplanar jets, the space angle between the directions of the total momenta in the two hemispheres (acollinearity angle) is required to be smaller than 165° , and the angle between the directions of these total momenta projected onto a plane transverse to the beam axis (acoplanarity angle) not to exceed 175° .

Finally, if one of the two hemispheres contains no charged particles, the total mass in each hemisphere is required to be smaller than 4 GeV/ c^2 . While this criterion largely

eliminates the background from $\tau\tau\gamma$ final states in which one of the two hemispheres contains only a radiated photon, it does not introduce any inefficiency for the signal since an A boson with mass in excess of $2m_\tau$ always has a negligible branching ratio into final states containing only neutral particles.

No events have been found in the data or in the standard process Monte Carlo samples. When combined with the search for the MSM Higgs boson in the configuration $(H \rightarrow \text{hadrons})(Z^* \rightarrow \nu\bar{\nu})$, the efficiency of this search is 39% for $m_h = 60 \text{ GeV}/c^2$ and $m_A = 6 \text{ GeV}/c^2$ (with a branching ratio of 85% for $A \rightarrow \tau^+\tau^-$).

The selection criteria for $(h \rightarrow AA)(Z^* \rightarrow e^+e^- \text{ or } \mu^+\mu^-)$ are listed below.

The total charged multiplicity must be 4 or 6, including tracks possibly coming from V^0 decays, and the total electric charge must be zero. Larger charged multiplicities are covered by the MSM Higgs boson search in the energetic lepton pair in hadronic events topology [4]. Again, no track may be reconstructed with $|\cos\theta| > 0.95$, and no energy may be detected within 12° of the beam axis.

The event must contain a charged particle pair satisfying the following conditions. The two particles must come from the beam crossing point and must have opposite electric charges. As in the search for energetic lepton pairs in hadronic events, both momenta are required to exceed $3 \text{ GeV}/c$, their scalar sum must be larger than $20 \text{ GeV}/c$, and the invariant mass of the pair must not be smaller than $5 \text{ GeV}/c^2$. The particles must be identified as two electrons or as two muons, at least one of them tightly, using the criteria applied in the corresponding MSM Higgs boson search [3]. Electrons belonging to an identified photon conversion are rejected.

The two lepton tracks are then removed, and the thrust axis of the rest of the event is determined. As in the search for energetic lepton pairs in hadronic events, the scalar sum of the transverse momenta of the two leptons, calculated with respect to that axis, is required to exceed $15 \text{ GeV}/c$. With the two leptons still removed, the event is divided into two hemispheres by a plane perpendicular to that same axis. In each hemisphere, the total electric charge is required to be equal to zero and the total energy to exceed 2 GeV . Hemispheres consisting of an identified photon conversion are rejected. In order to remove the large fraction of the background from $l^+l^-\bar{f}\bar{f}\gamma$ final states in which the $\bar{f}\bar{f}$ or the photon direction is close to that of one of the leptons, all masses obtained by combining a lepton with the content of an hemisphere are required to be larger than $2 \text{ GeV}/c^2$.

Finally, if one of the two hemispheres contains no charged particles, the total mass in each hemisphere is again required to be smaller than $4 \text{ GeV}/c^2$.

Requiring, as in the MSM Higgs boson search, the mass recoiling against the lepton pair to be larger than $40 \text{ GeV}/c^2$, no events have been found in the data, and none in the standard process Monte Carlo samples either. When combined with the search for the MSM Higgs boson in the configuration $(H \rightarrow \text{hadrons})(Z^* \rightarrow e^+e^- \text{ or } \mu^+\mu^-)$, the efficiency of this search is 45% for $m_h = 60 \text{ GeV}/c^2$ and $m_A = 6 \text{ GeV}/c^2$ (with a branching ratio of 85% for $A \rightarrow \tau^+\tau^-$).

If the cut on the recoil mass is removed, two events are selected, with recoil masses of 7.5 and 12.5 GeV/ c^2 . In both cases, one of the hemispheres does not contain any charged particles. These two events can be interpreted as coming from the reactions $e^+e^- \rightarrow l^+l^- \bar{f}\bar{f}\gamma$, with one of the hemispheres consisting of a single photon and the other of the $\bar{f}\bar{f}$ system. Indeed, ~ 2 such events are expected to be selected in the full data sample, according to simulations performed with the FERMISV four-fermion final state generator [11] which includes initial and final state radiation. It is because of this background that the search with energetic lepton pairs has been restricted to recoil masses above 40 GeV/ c^2 .

The overall search efficiency obtained when $h \rightarrow AA$ is similar to the one achieved for a MSM Higgs boson when $m_A \gtrsim 2m_b$, and lower by no more than 10%, in relative value, for lower A masses. For $m_A < 2m_\tau$, this is due in particular to the fact that the fraction of final states containing no charged particles in a $h \rightarrow AA$ decay never exceeds 13%, a maximum which is reached, given the decay channels allowed for a CP-odd Higgs boson in this mass range [10], when both A bosons decay into $\eta\eta\eta$.

As a result, the 95% CL upper limit on ξ^2 obtained in the previous section and shown in Fig. 1 applies in the present context for $m_A \gtrsim 2m_b$, and is degraded by at most 10% otherwise, in which case the lower limit on m_h is reduced to 57.8 GeV/ c^2 for $\xi^2 = 1$.

4. Search for an invisible Higgs boson

The topologies associated with the production of an invisible Higgs boson h in the reaction $e^+e^- \rightarrow hZ^*$ depend on the decay channel and on the mass of the Z^* . They are:

- a purely invisible final state in the 20% of cases in which $Z^* \rightarrow \nu\bar{\nu}$;
- an acoplanar lepton pair in the 10% of cases in which $Z^* \rightarrow l^+l^-$;
- an acoplanar pair of jets or a monojet, depending whether the Z^* mass is large or small compared to its momentum, in the remaining 70% of cases in which $Z^* \rightarrow$ hadrons.

The purely invisible final state contributes far too little to the Z invisible width to be useful. The search for acoplanar jets, optimized for the case of a high mass standard model Higgs boson produced in the reaction $e^+e^- \rightarrow H\nu\bar{\nu}$ and decaying into hadrons, is described in Ref. 4. No candidate events were found. The results can be reinterpreted in the present context, with the rôles of the Higgs boson and of the Z^* simply interchanged.

The search for monojets, complemented by the search for acoplanar pairs described below, was optimized for a low mass Higgs boson produced in the same reaction. The selection criteria listed below are identical to those described in Ref. 3.

The charged multiplicity must be at least 4. (Monojets containing only two charged particles are treated as acoplanar lepton pairs, as described below.) The events are divided into two hemispheres by a plane perpendicular to the thrust axis, and one of the two hemispheres is required to contain an energy smaller than 2 GeV while the other hemisphere is called the monojet. In order to ensure that the final state is

well contained in the detector, it is required that $|\cos\theta| < 0.9$ for the monojet, and that no energy be measured within 12° of the beam axis. A clear monojet topology is achieved by the requirement that the cone of half-opening angle 50° around the direction opposite to that of the monojet contain no energy.

At this stage, most of the remaining background comes from two-photon processes and is largely reduced by the requirement that the component of the total momentum transverse to the beam direction exceed 5% of the centre-of-mass energy. To eliminate the few events surviving in the standard two-photon process Monte Carlo samples, the projected acoplanarity ψ_p is required to be smaller than 150° . Here, ψ_p is calculated as follows: all particle momenta are projected onto a plane perpendicular to the beam axis; a 2d-thrust axis is computed from these projections; the event is divided into two 2d-jets by a line perpendicular to that axis; ψ_p is the angle between the directions of these two 2d-jets (for 2d-monojets, ψ_p is set to zero).

No monojet candidate events were found in the data or in the standard process Monte Carlo samples.

The selection criteria for acoplanar lepton pairs, updated from Ref. 3, are described below.

The topology of interest consists of a pair of charged particles or τ decay products accompanied by missing energy. Events with 2 or 4 charged particle tracks and total electric charge zero are considered. Triplets of tracks with an invariant mass smaller than $1.5 \text{ GeV}/c^2$ are selected as τ candidates. If more than one triplet fulfils these conditions, only the one with the lowest mass is considered. For simplicity, the τ triplets and the remaining charged particle tracks are referred to as leptons, and only the events with two leptons are further considered. In order to avoid energy losses in the very forward and backward directions, it is required that no energy be detected within 12° of the beam axis, and that $|\cos\theta| < 0.95$ for each lepton.

To reduce the large $Z \rightarrow l^+l^-$ background, it is required that the angle between the two lepton directions be smaller than 165° . Events from $Z \rightarrow l^+l^- \gamma$ are eliminated by a “photon veto”. An event is vetoed if it contains a neutral particle with energy above 1 GeV. In order not to veto acoplanar τ pairs, neutral particles with a momentum direction closer than 10° to that of one of the leptons or which form an invariant mass smaller than $2 \text{ GeV}/c^2$ with one of the leptons are not considered in the veto procedure. In order to retain efficiency for low multiplicity monojets, the photon veto is applied only if the total visible mass of the event exceeds $10 \text{ GeV}/c^2$.

The component of the vector sum of the lepton momenta transverse to the beam axis must exceed 5% of the centre-of-mass energy. The same cut is applied to the transverse component of the total visible momentum. These missing transverse momentum cuts eliminate most of the background from the two-photon processes $\gamma\gamma \rightarrow l^+l^-$. However, some events from $\gamma\gamma \rightarrow \tau^+\tau^-$ are expected to survive because of the transverse momentum carried away by the τ -decay neutrinos. To eliminate this background, the following procedure is applied: the lepton momenta are projected onto a plane perpendicular to the beam axis, and a 2d-thrust axis is computed from these projections;

the scalar sum of the transverse components of the 2d-lepton momenta, measured with respect to the 2d-thrust axis, is required to be larger than $2 \text{ GeV}/c$.

This last cut is not applied if the event is monojet-like, *i.e.* if the 2d-thrust axis points between the two projected lepton momenta. In such a case, criteria designed for the monojet search are applied instead: the monojet direction must have $|\cos\theta| < 0.9$, the hemisphere opposite to the monojet direction must not contain an energy exceeding 2 GeV , and no energy may be detected in the cone of half-opening angle 50° around the direction opposite to that of the monojet. Finally, the monojet must not consist of an identified photon conversion.

No events have been selected in the standard process Monte Carlo samples, but a very acoplanar e^+e^- pair, shown in Fig. 2, was found in the data. The mass recoiling against the two leptons, *i.e.* the mass of the invisible Higgs boson candidate, is $61.3 \text{ GeV}/c^2$, with a resolution of $0.6 \text{ GeV}/c^2$. This event lies far from all the selection cuts. Its salient features are an e^+e^- mass m of $3.31 \pm 0.02 \text{ GeV}/c^2$ and a missing transverse momentum p_t of $20.3 \text{ GeV}/c$. Within the standard model, its most likely origin is the process $e^+e^- \rightarrow l^+l^- \nu\bar{\nu}$. The expected number of such events and their kinematic characteristics have been evaluated using the FERMISV generator. When the three lepton flavours are combined, a total of ~ 0.9 such events is expected to be selected (with an additional ~ 0.5 if $q\bar{q}\nu\bar{\nu}$ final states are included). While this is in agreement with the observation of one event, the process $e^+e^- \rightarrow l^+l^- \nu\bar{\nu}$ tends to produce events which cluster toward the lowest m and p_t values. The probability for such an event, once selected, to lie beyond $3 \text{ GeV}/c^2$ in mass and $20 \text{ GeV}/c$ in transverse momentum is found to be 0.3% . The probability for an event to show up in as unlikely a configuration (maybe more unlikely in m and less in p_t , or the reverse) is 2% . On the other hand, if this event were to be interpreted as coming from the process $e^+e^- \rightarrow h e^+e^-$, the value of the mass of the e^+e^- pair would be unexpectedly low, with a probability of only 1% .

Calculated with respect to all hZ^* final states, the combined efficiency of the searches for acoplanar lepton pairs, for monojets and for acoplanar jets increases smoothly from 10% for a massless Higgs boson to 50% for $m_h = 45 \text{ GeV}/c^2$ and then decreases slowly to 40% for $m_h = 70 \text{ GeV}/c^2$. The 95% CL upper limit on the ratio ξ^2 of the production cross-section of such an invisible Higgs boson to the corresponding cross-section for a minimal standard model Higgs boson is presented in Fig. 1, as a function of m_h . The cusp at $m_h = 61.3 \text{ GeV}/c^2$ is due to the candidate event, with the mass information taken into account according to the prescription of Ref. 12. For $m_h = 0$, ξ^2 is constrained to be smaller than $2.3 \cdot 10^{-3}$. For $\xi^2 = 1$, the lower limit on m_h is $65 \text{ GeV}/c^2$. This seemingly large value is due to the fact that, in contrast to the MSM Higgs boson case, the hadronic Z^* decays can be used in the search for an invisible Higgs boson.

If only a fraction f_{inv} of the Higgs boson decays is invisible, the upper limit ξ^2_{mix} on ξ^2 lies between ξ^2_{inv} , the limit obtained here for a purely invisible Higgs boson, and ξ^2_{vis} , the limit obtained in Section 2 or in Section 3, depending on whether h does not or does decay into AA. The actual value is given by $1/\xi^2_{mix} = f_{inv}/\xi^2_{inv} + (1 - f_{inv})/\xi^2_{vis}$.

5. Implications in the MSSM

The Higgs sector of the MSSM is highly constrained [1]. At tree level, all masses and all couplings depend on only two parameters which can conveniently be chosen as m_h and m_A . However, because of the large value of the top quark mass m_t , one-loop radiative corrections to the CP-even squared mass matrix must be taken into account [13]. Assuming for simplicity that the scalar partners \tilde{t} of the top quark are mass degenerate, these corrections can be parametrized as $\varepsilon_0/\sin^2\beta$, with [14]

$$\varepsilon_0 = \frac{3g^2}{8\pi^2} \frac{m_t^4}{m_W^2} \log \frac{m_{\tilde{t}}^2}{m_t^2}.$$

For the “typical” set of values $m_t = 140 \text{ GeV}/c^2$ and $m_{\tilde{t}} = 1 \text{ TeV}/c^2$, $\varepsilon_0 = (60 \text{ GeV}/c^2)^2$. As in any two-doublet model, the ZZh and ZhA couplings are proportional to $\sin(\beta-\alpha)$ and to $\cos(\beta-\alpha)$, respectively. Therefore, searches for the bremsstrahlung process $e^+e^- \rightarrow hZ^*$ and for the associated production process $e^+e^- \rightarrow hA$ are complementary. In the rest of this section, the usual assumption that $\tan\beta$ is larger than unity is made, as suggested by the large ratio of the top to the bottom-quark masses.

Let it first be assumed that decay modes into supersymmetric particles are unavailable, in particular invisible decay modes. The ξ^2 limits obtained in Sections 2 and 3 can be used to reduce the allowed domain in the (m_h, m_A) plane, as shown in Fig. 3a for the typical set of parameters. The searches for signals of associated production of h and A in the data sample collected by ALEPH in 1989 and 1990 have been described in Ref. 3, and updated as reported in Ref. 15 to include the data accumulated in 1991. The resulting exclusion domain is shown in Fig. 3b for the typical set of parameters. Since the associated production process is already kinematically limited, in contrast to the bremsstrahlung process, there remains little to gain from the analysis of more data. Combining the two sets of results, the domain shown in Fig. 3c is excluded, which allows mass lower limits of 44.5 and 45 GeV/c^2 to be derived for m_h and m_A , respectively.

These limits are however valid only for the typical choice of parameters, $m_t = 140 \text{ GeV}/c^2$ and $m_{\tilde{t}} = 1 \text{ TeV}/c^2$. The effect of varying these parameters is demonstrated in Figs. 3d and 3e, obtained with $m_t = 100$ and $180 \text{ GeV}/c^2$, respectively (and keeping the $m_{\tilde{t}}/m_t$ ratio fixed). While the lower bound on m_h is hardly affected, the lower bound on m_A is degraded for large m_t values. The set of points in the (m_h, m_A) plane which is excluded irrespective of the values taken by m_t and by $m_{\tilde{t}} > m_t$ is limited by curve (A) in Fig. 3f. This boundary comes: *i*) on the left side from the negative search for $Z \rightarrow hZ^*$, interpreted in the case of a very light top quark ($\varepsilon_0 = 0$); *ii*) on the right side from the theory, in the case of a very heavy top quark ($\varepsilon_0 \rightarrow \infty$); *iii*) on the low side from the negative search for $Z \rightarrow hA$, along the kinematic limit for this process. It can be seen that, in all cases, m_h and m_A have to exceed 44 and 21 GeV/c^2 , respectively. The particular cases of long-lived Higgs bosons with masses smaller than $2m_\mu$ are either unphysical in the case of h , as can be seen in Fig. 3, or already excluded by dedicated searches [8] in the case of A .

Given the present limits on supersymmetric particles [3], Higgs boson decays into such particles are not relevant in the mass range considered here, except possibly for the invisible modes (h or A) $\rightarrow \chi\chi$. Indeed, LEP data exclude $m_\chi \lesssim 15 \text{ GeV}/c^2$ for $\tan\beta \gtrsim 2$ [3], while the limits obtained for the gluino mass in $p\bar{p}$ collisions [16] can be used in the MSSM framework to extend the $15 \text{ GeV}/c^2$ lower limit on m_χ into the $1 < \tan\beta < 2$ region. These constraints do not forbid *e.g.* $h \rightarrow \chi\chi$ if $m_h = 50 \text{ GeV}/c^2$ and $m_\chi = 20 \text{ GeV}/c^2$. In addition, there remains a so-called “light gluino window” in the mass region 3 to 4 GeV/c^2 which is not fully excluded experimentally. As a consequence, the possibility of a very light χ , with $\tan\beta$ close to unity, should not be overlooked. This means that invisible decay modes should be considered for any Higgs boson masses, especially in view of their potentially large branching ratios [6].

If h can decay invisibly, the domain shown in Fig. 3a, excluded for the typical set of parameters by the search for $e^+e^- \rightarrow hZ^*$, can only become larger since the limits obtained on ξ^2 are tighter for an invisible than for a visible Higgs boson. On the other hand, the searches for $e^+e^- \rightarrow hA$ described in Ref. 3 become inefficient, and the results displayed in Fig. 3b are no longer valid. Constraints resulting from the Z width measurement can however be used in this case too, as explained in Ref. 3, and the practical result is that the window at low h and A masses which is visible in Fig. 3a becomes closed. The set of points which is excluded, whatever the invisible fractions of h and A decays, when m_t and $m_{\tilde{t}} > m_t$ are allowed to vary arbitrarily, is limited by curve (B) in Fig. 3f.

6. Conclusions

Searches have been performed for signals of the production of a non-minimal CP-even Higgs boson h in the bremsstrahlung process $e^+e^- \rightarrow hZ^*$. Only one candidate event was found, an acoplanar e^+e^- pair which may be interpreted at the few percent probability level as coming from the process $e^+e^- \rightarrow e^+e^- \nu\bar{\nu}$.

Limits on ξ^2 , the ratio of the $e^+e^- \rightarrow hZ^*$ production cross-section to its MSM equivalent, have been derived as a function of m_h in the cases where h decays like an MSM Higgs boson, with possibly modified branching ratios, into a pair of A bosons, or into invisible final states. For a purely invisible Higgs boson produced with the same cross-section as in the MSM, the mass lower limit is $65 \text{ GeV}/c^2$.

Together with previous ALEPH results on the associated production process $e^+e^- \rightarrow hA$, these limits exclude a domain in the (m_h, m_A) plane of the MSSM, the area of which depends on the size of the radiative corrections to the CP-even squared mass matrix and on the availability of supersymmetric decay modes. If such decay modes are forbidden, mass lower limits of 44.5 and $45 \text{ GeV}/c^2$ result for the h and A bosons, respectively, assuming $m_t = 140 \text{ GeV}/c^2$, $m_{\tilde{t}} = 1 \text{ TeV}/c^2$ and $\tan\beta > 1$. If m_t and $m_{\tilde{t}} > m_t$ are allowed to vary arbitrarily, these limits become 44 and $21 \text{ GeV}/c^2$, respectively.

These results improve on those obtained in previous analyses [3,17], and are the first ones reported in the case of invisible Higgs decays.

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Figure Captions

1. As a function of m_h , the 95% CL upper limit on ξ^2 , the ratio of the production cross-section of a non-minimal CP-even Higgs boson h in the reaction $e^+e^- \rightarrow hZ^*$ to the corresponding cross-section for a MSM Higgs boson.

Curve (A) applies if h decays into the same final states as an MSM Higgs boson, with modified branching ratios; the discontinuities correspond to thresholds for various h decay modes ($\pi\pi$, $K\bar{K}$, $\tau^+\tau^-$ and $c\bar{c}$, and $b\bar{b}$), except for the one at $40 \text{ GeV}/c^2$ which is related to the recoil mass cut in the $h1^+1^-$ channel; there is no general upper limit on ξ^2 for $m_h < 2m_\mu$. If h decays into AA , the limit (A) holds if $m_A \gtrsim 2m_b$; this limit is degraded (*i.e* translated upwards) by no more than 10% for lower A masses.

Curve (B) applies if h decays invisibly; the cusp at $61.3 \text{ GeV}/c^2$ corresponds to the candidate acoplanar e^+e^- pair.

2. The selected acoplanar e^+e^- pair. The mass of the pair is $3.31 \text{ GeV}/c^2$, its transverse momentum is $20.3 \text{ GeV}/c$, and the mass of the invisible system recoiling against the e^+e^- pair is $61.3 \text{ GeV}/c^2$.

3. Excluded domains in the (m_h, m_A) plane of the MSSM:

- a) from the search for $Z \rightarrow hZ^*$,
- b) from the search for $Z \rightarrow hA$, and
- c) from these two searches combined,

all for the typical values $m_t = 140 \text{ GeV}/c^2$ and $m_{\tilde{\tau}} = 1 \text{ TeV}/c^2$, for $\tan\beta > 1$, and assuming no invisible Higgs boson decays.

The same as (c):

- d) for $m_t = 100 \text{ GeV}/c^2$, and
- e) for $m_t = 180 \text{ GeV}/c^2$,

both with $m_{\tilde{\tau}}/m_t$ as in (c).

f) Limited by curve (A), the domain excluded for any m_t or $m_{\tilde{\tau}} > m_t$ values, assuming no invisible Higgs boson decays; limited by curve (B), the same, now allowing for arbitrary fractions of invisible h and A decays.

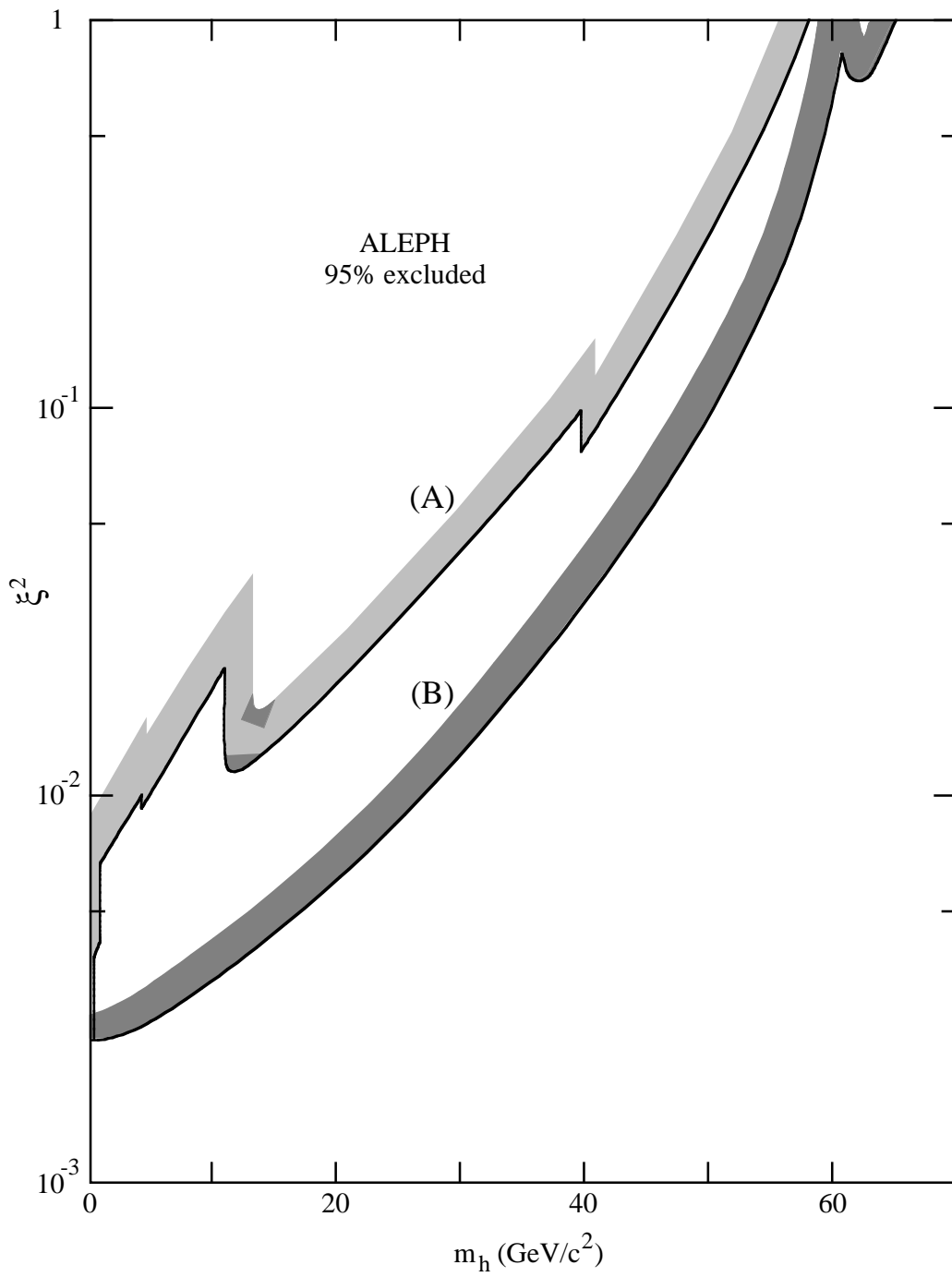


Figure 1

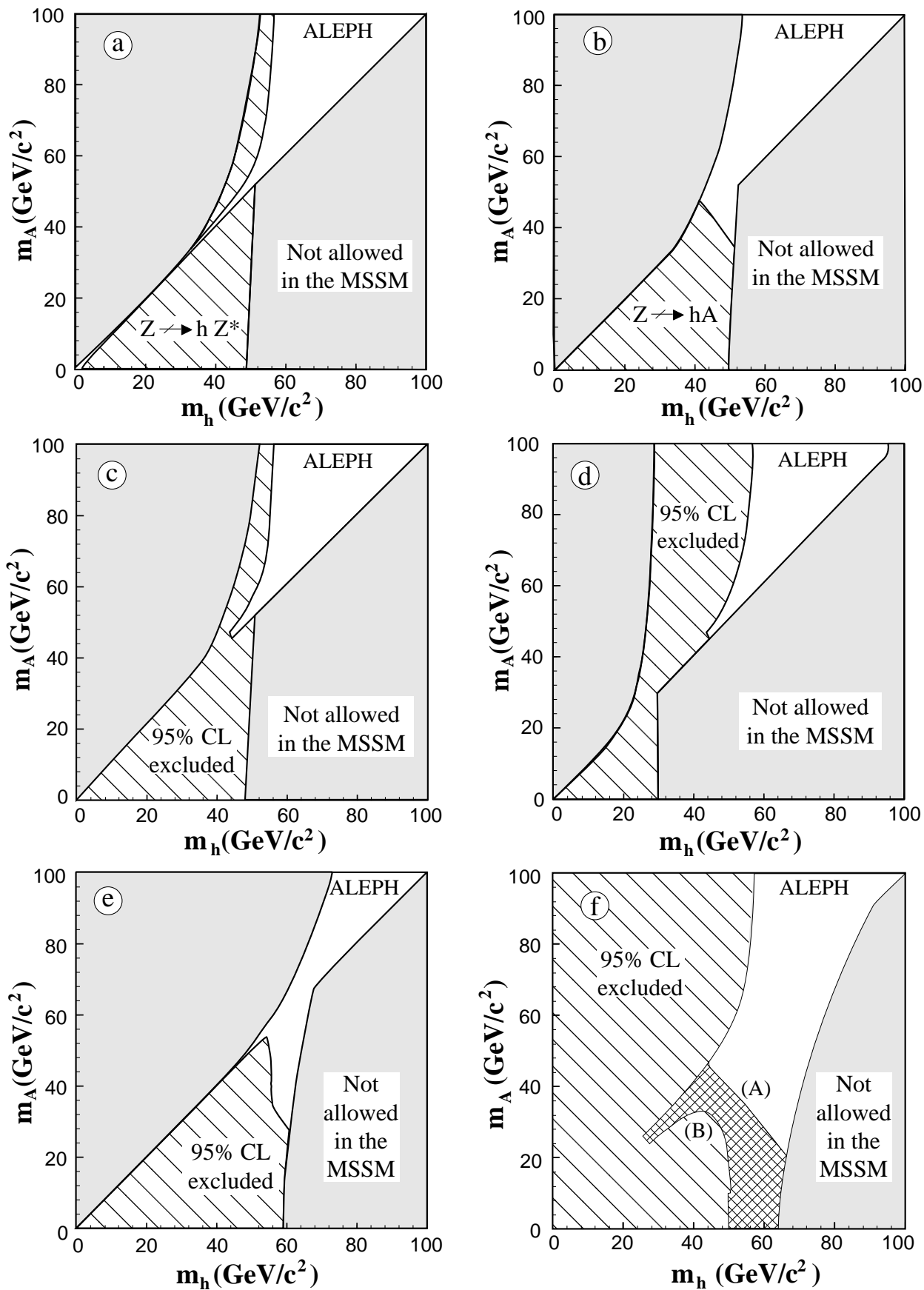


Figure 3